

Millersville University
 Department of Mathematics
 MATH 365, *Ordinary Differential Equations*, Homework 01
 January 14, 2009

Name _____

Please answer the following questions. Answers without justifying work will receive no credit. Partial credit will be given as appropriate, do not leave any problem blank. Each problem is worth 10 points. Your completed assignment is due at class time on Friday, January 16, 2009.

1. Please complete the following table. In each case y is the dependent variable and t is the independent variable. All other letters represent constants.

Differential Equation	Order	Linear ? (y/n)	Autonomous ? (y/n)
$y'' = -ky$			
$ty'' + y' + ty = 0$			
$y + ty' = y^2$			
$E I y^{(4)} = f(t)$			
$y'' + 4y' + 5y = 100 \sin 20t$			
$y'' = \frac{w}{H} \sqrt{1 + (y')^2}$			

2. Determine if $y(t) = e^{-t} + t - 1$ is a solution to the ordinary differential equation

$$y' + y = t.$$

3. Determine if $y(t) = c_1e^{-2t} + c_2e^t + c_3e^{3t}$ is a solution to the ordinary differential equation

$$y''' - 2y'' - 5y' + 6y = 0.$$

The expressions c_i for $i = 1, 2, 3$ are constants.

4. Determine if $y(t) = At^3 + Bt^{-4} - \frac{1}{3}t^2$ is a solution to the ordinary differential equation

$$t^2y'' + 2ty' - 12y = 2t^2.$$

The symbols A and B are constants.

5. A change of variable can sometimes enable us to switch the roles of the independent and dependent variables in an ordinary differential equation. Starting with the equation

$$\frac{dy}{dt} = \frac{1}{\frac{dt}{dy}}$$

differentiate both sides with respect to t to show that

$$\frac{d^2y}{dt^2} = -\frac{\frac{d^2t}{dy^2}}{\left(\frac{dt}{dy}\right)^3}.$$

6. Use the identity established in exercise 5 to re-write the following ordinary differential equation as one with t as the independent variable.

$$\frac{d^2 t}{dy^2} + (\sin t) \left(\frac{dt}{dy} \right)^3 = 0$$